

## 201-203-RE - Supplement A - Definite Integrals and Areas

Approximate the following integrals using the Right-End Point method with the given  $n$ . Round your answers to 4 decimals.

$$(1) \int_1^4 \frac{2}{4x^2 + 9} dx \quad n = 6$$

$$(10) \int_0^{12} \frac{5}{\ln(x+2)} dx \quad n = 6$$

$$(2) \int_1^3 (\ln(x) + 3)^2 dx \quad n = 4$$

$$(11) \int_0^8 \cos(x^2 + x) dx \quad n = 4$$

$$(3) \int_2^4 \frac{6}{\sqrt{1 + \ln(x)}} dx \quad n = 4$$

$$(12) \int_1^{13} \frac{x^2 + 1}{x^3 + 1} dx \quad n = 4$$

$$(4) \int_{-2}^2 (x^3 + 6)^{2/3} dx \quad n = 4$$

$$(13) \int_0^4 e^{\cos(3x)} dx \quad n = 4$$

$$(5) \int_2^6 \frac{10}{\sqrt{x^2 + 4}} dx \quad n = 4$$

$$(14) \int_0^6 \sin\left(\frac{x^3}{3}\right) dx \quad n = 6$$

$$(6) \int_1^9 \sqrt[5]{x^2 + 3x} dx \quad n = 8$$

$$(15) \int_0^1 \sqrt{\cos(x)} dx \quad n = 4$$

$$(7) \int_4^{10} \sqrt[3]{x^2 + 5} dx \quad n = 6$$

$$(16) \int_1^5 \cos(e^{1-x}) dx \quad n = 4$$

$$(8) \int_2^7 \frac{e^{3-x}}{\ln(x)} dx \quad n = 4$$

$$(17) \int_0^4 e^{\sin(x)} dx \quad n = 4$$

$$(9) \int_0^3 \sqrt{x^2 + 2x} dx \quad n = 6$$

$$(18) \int_{-1}^2 \sqrt{1 + e^x} dx \quad n = 6$$

(19) Given the following graph of  $f$ , find:

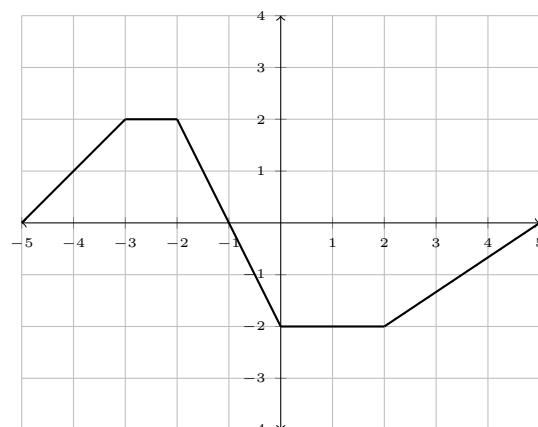
$$(a) \int_{-5}^{-3} f(x) dx$$

$$(d) \int_{-1}^2 f(x) dx$$

$$(b) \int_{-5}^{-1} f(x) dx$$

$$(e) \int_{-5}^5 f(x) dx$$

$$(c) \int_{-3}^1 f(x) dx$$



(20) Given the following graph of  $f$ , find:

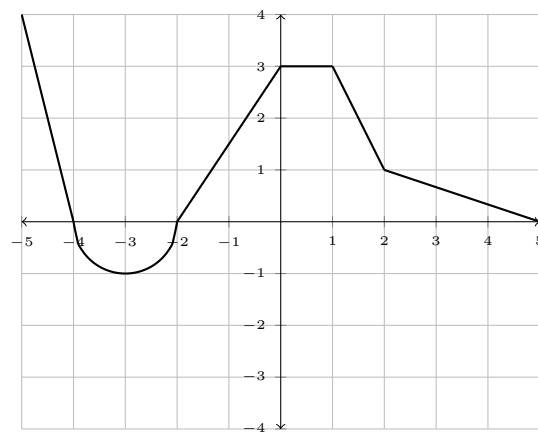
$$(a) \int_{-5}^{-2} f(x) dx$$

$$(d) \int_{-2}^2 f(x) dx$$

$$(b) \int_{-3}^0 f(x) dx$$

$$(e) \int_{-5}^5 f(x) dx$$

$$(c) \int_{-1}^1 f(x) dx$$



(21) Given the following graph of  $f$ , find:

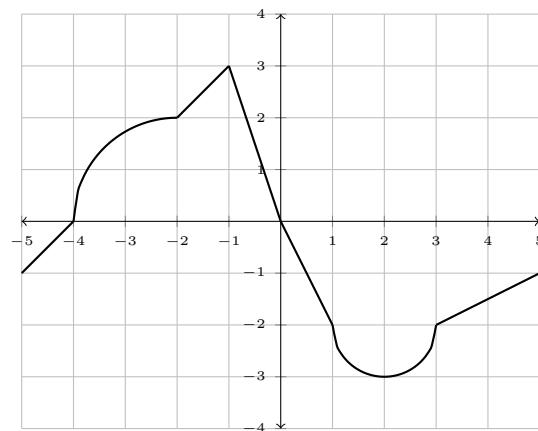
$$(a) \int_{-5}^{-2} f(x) dx$$

$$(d) \int_0^5 f(x) dx$$

$$(b) \int_0^{-4} f(x) dx$$

$$(e) \int_{-5}^5 f(x) dx$$

$$(c) \int_{-1}^1 f(x) dx$$



(22) Given the following graph of  $f$ , find:

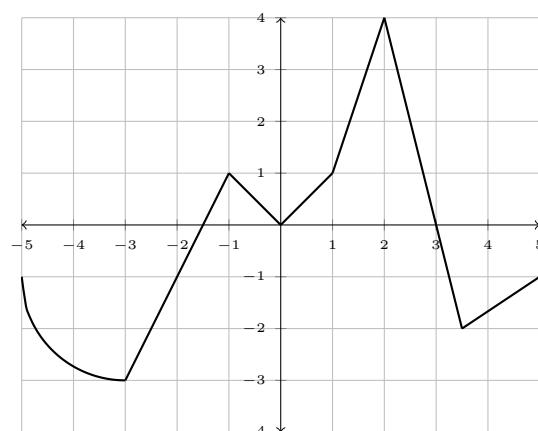
$$(a) \int_{-3}^{-5} f(x) dx$$

$$(d) \int_2^5 f(x) dx$$

$$(b) \int_{-5}^0 f(x) dx$$

$$(e) \int_{-5}^5 f(x) dx$$

$$(c) \int_0^2 f(x) dx$$



(23) Given the following graph of  $f$ , find:

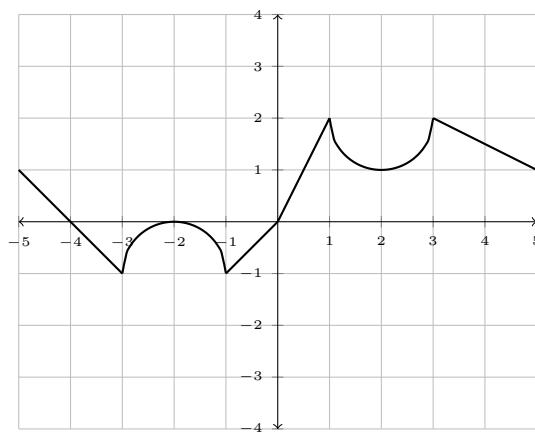
$$(a) \int_{-5}^{-1} f(x) dx$$

$$(d) \int_0^5 f(x) dx$$

$$(b) \int_1^{-3} f(x) dx$$

$$(e) \int_{-5}^5 f(x) dx$$

$$(c) \int_{-1}^3 f(x) dx$$



(24) Given the following graph of  $f$ , find:

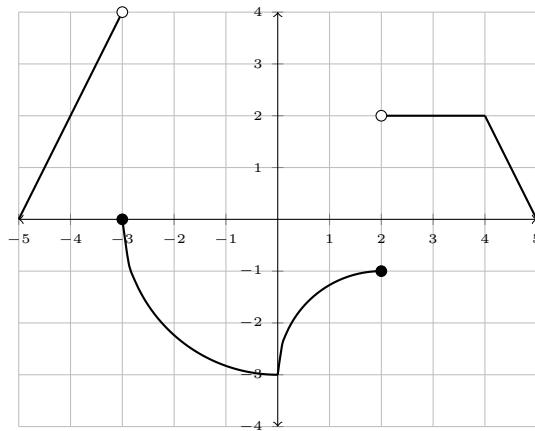
$$(a) \int_{-5}^0 f(x) dx$$

$$(d) \int_2^2 f(x) dx$$

$$(b) \int_{-3}^2 f(x) dx$$

$$(e) \int_{-5}^5 f(x) dx$$

$$(c) \int_0^3 f(x) dx$$



### ANSWERS:

(1) 0.1781      (4) 15.6940      (7) 23.5685      (10) 29.7600      (13) 5.7111      (16) 3.9225

(2) 28.6862      (5) 8.4477      (8) 1.0688      (11) 0.0020      (14) 1.3266      (17) 6.4231

(3) 8.1789      (6) 16.9650      (9) 7.5984      (12) 1.7554      (15) 0.8779      (18) 5.7376

(19) (a) 2      (b) 5      (c) 0      (d) -5      (e) -3

(20) (a)  $2 - \frac{\pi}{2}$       (b)  $3 - \frac{\pi}{4}$       (c)  $\frac{21}{4}$       (d) 8      (e)  $\frac{23}{2} - \frac{\pi}{2}$

(21) (a)  $\pi - \frac{1}{2}$       (b)  $-\pi - 4$       (c)  $\frac{1}{2}$       (d)  $-8 - \frac{\pi}{2}$       (e)  $\frac{\pi}{2} - \frac{9}{2}$

(22) (a)  $2 + \pi$       (b)  $-\pi - \frac{7}{2}$       (c) 3      (d)  $-\frac{3}{4}$       (e)  $-\pi \frac{5}{4}$

(23) (a)  $\frac{\pi}{2} - 2$       (b)  $\frac{3}{2} - \frac{\pi}{2}$       (c)  $\frac{9}{2} - \frac{\pi}{2}$       (d)  $8 - \frac{\pi}{2}$       (e)  $\frac{11}{2}$

(24) (a)  $4 - \frac{9\pi}{4}$       (b)  $-6 - \frac{5\pi}{4}$       (c)  $\pi - 4$       (d) 0      (e)  $3 - \frac{5\pi}{4}$